Existence results of a singular fractional differential equation with perturbed term

¹Rym Bourguiba, ^{1,2}Faten Toumi ¹Monastir, Tunisia, ²Kairouan, Tunisia

This paper is devoted to the study of the following nonlinear fractional differential equation with perturbed term

$$\begin{cases} D^{\alpha}u(t) + \mu a(t)f(t, u(t)) - q(t) = 0, & \text{in } (0, 1), \\ u(0) = u'(0) = \dots = u^{(n-2)}(0) = 0, & u(1) = \lambda \int_0^1 u(s)ds, \end{cases}$$

depending on the real parameter $\mu > 0$, where $n \in \mathbb{N}$, $n \ge 3$, $n - 1 < \alpha \le n$, $0 < \lambda < \alpha$, D^{α} denotes the Reimann-Liouville derivative of order α . The function a is continuous nonnegative on (0, 1) and it is allowed to be singular at t = 0 and/or t = 1. The function f is in $\mathcal{C}([0, 1] \times [0, +\infty), [0, +\infty))$. The perturbed term $q : (0, 1) \rightarrow [0, +\infty)$ is measurable function and satisfies some properties detailed below. Throughout our nonlinearity may change sign. In this work various existence and multiplicity results for positive solutions are derived depending of different values of the parameter μ . Some illustrative examples are also discussed.

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